► JOHN BALDWIN, On strongly minimal Steiner systems:

 ${\it Zilber's\ conjecture,\ universal\ algebra,\ and\ combinatorics.}$

Mathematics, Statistics and Computer Science, University of Illinois at Chicago, 850 S. Morgan St. Chicago IL 60607,USA.

E-mail: jbaldwinQuic.edu.

URL Address: http://homepages.math.uic.edu/ jbaldwin/. With Gianluca Paolini [BP18], we constructed, using a variant on the Hrushovski dimension function, for every $k \geq 3$, 2^{μ} families of strongly minimal Steiner k-systems. We study the mathematical properties of these counterexamples to Zilber's trichotomy conjecture rather than thinking of them as merely exotic examples. In particular the long study of finite Steiner systems is reflected in results that depend on the block size k. A quasigroup is a structure with a binary operation such that for each equation xy = z the values of two of the variables determines a unique value for the third. The new Steiner 3-systems are bi-interpretable with strongly minimal Steiner quasigroups. For k > 3, we show the pure k-Steiner systems have 'essentially unary definable closure' and do not interpret a quasigroup. But we show that for q a prime power the Steiner q-systems can be interpreted into specific sorts of quasigroups, block algebras. This show a dichotomy within the class of strongly minimal sets with flat geometries.

We extend the notion of an (a, b)-cycle graph arising in the study of finite and infinite Stein triple systems ([CW12]) by introducing what we call the (a, b)-path graph of a block algebra. We exhibit theories of strongly minimal block algebras where all (a, b)paths are infinite and others in which all are finite only in the prime model. We show how to obtain combinatorial properties (e.g. 2-transitivity) by either varying the basic collection of finite partial Steiner systems or modifying the μ function which ensures strong minimality.

[BP18]John T. Baldwin and G. Paolini. Strongly Minimal Steiner Systems I. submitted, 2018.

[CW12]P. J. Cameron and B. S. Webb. Perfect countably infinite Steiner triple systems. *Australas. J. Combin.*, 54:273–278, 2012.